**Aim:** Implementing the Longest Common Sub-sequence using Dynamic Programming Approach

**IDE:** Visual Studio Code

### Longest Common Sub-sequence

### Theory: -

### The Longest Common Subsequence (LCS) problem is a classic problem in computer science and bioinformatics that involves finding the longest sequence that can be derived from two given sequences without altering the order of their elements. It is an important problem in string processing and is widely used in applications such as text comparison, DNA sequence analysis, and data diffing tools.

### 1. Problem Definition

### Given two sequences, the task is to find the longest subsequence that is present in both sequences. A subsequence is a sequence derived by deleting some or no elements from the original sequence without rearranging the order of the remaining elements.

### For example:

### Sequence 1: "abcde"

### Sequence 2: "ace"

### The LCS is "ace" because it is the longest sequence that appears in the same order in both.

### 2. Applications of LCS

### Text comparison: Helps detect similarities between text files or documents.

### DNA sequence alignment: Identifies common patterns in genetic sequences.

### Version control systems: Finds differences between versions of files.

### Spell checkers: Matches words with similar spellings.

### 3. Approach to find LCS :-

### The most common approach to solving the LCS problem is using Dynamic Programming.

### Define a DP table: Create a table where each cell represents the length of the LCS for two substrings of the input sequences.

### Initialize the table: Set the first row and column to 0 since the LCS of any sequence with an empty sequence is 0.

### Use a recurrence relation:

### If the current characters of both sequences match: dp[i][j]=dp[i−1][j−1]+1

### If they don’t match: dp[i][j]=max(dp[i−1][j],dp[i][j−1])

### Retrieve the result: The value in the bottom-right cell of the table gives the length of the LCS.

### Algorithm: -

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### Programming Language: - C++

### Code :-

### #include<bits/stdc++.h>

### using namespace std;

### string Longest\_Common\_Subsequence(string X, string Y) {

### int m = X.length();

### int n = Y.length();

### int dp[m + 1][n + 1];

### for (int i = 0; i <= m; i++) {

### for (int j = 0; j <= n; j++) {

### if (i == 0 || j == 0) {

### dp[i][j] = 0;

### }

### else if (X[i - 1] == Y[j - 1]) {

### dp[i][j] = dp[i - 1][j - 1] + 1;

### }

### else {

### dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);

### }

### }

### }

### string lcsString;

### int i = m, j = n;

### while (i > 0 && j > 0) {

### if (X[i - 1] == Y[j - 1]) {

### lcsString = X[i - 1] + lcsString;

### i--;

### j--;

### }

### else if (dp[i - 1][j] > dp[i][j - 1]) {

### i--;

### }

### else {

### j--;

### }

### }

### return lcsString;

### }

### int main() {

### string X, Y;

### cout << "Enter The First String :- ";

### cin >> X;

### cout << "Enter The Second String :- ";

### cin >> Y;

### string result = Longest\_Common\_Subsequence(X, Y);

### cout << "Length of LCS is " << result.length() << endl;

### cout << "LCS is: " << result << endl;

### return 0;

### }

### Output :-

### Space Complexity:- \_\_\_\_\_\_\_\_\_ Justification: -

### \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

### Time Complexity:

### Best Case Time Complexity: \_\_\_\_\_\_\_\_\_ Justification: -

### \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

### Worst Case Time Complexity:- \_\_\_\_\_\_\_\_\_\_\_ Justification: -

### \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

### Conclusion:-

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